

# CI / Hypothesis test handout

Math 382

## t-Test for the mean

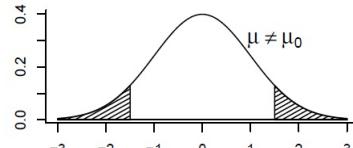
**Step 1.** Null Hypothesis  $H_0 : \mu = \mu_0$

**Step 2.** Alternative Hypothesis  $H_1 : \mu \neq \mu_0$  two-sided

**Step 3.** Critical value:  $t_{\alpha/2}$  with  $\text{df} = n - 1$

**Step 4.** Test Statistic  $t = \frac{\sqrt{n}(\bar{X} - \mu_0)}{s}$

**Step 5.** Decision Rule: Reject  $H_0$  if  $|t| > t_{\alpha/2}$



**Step 6.** (optional) p-value =  $2 \times P(T > |t|)$

Reject  $H_0$  when p-value <  $\alpha$

**Step 7.** Conclusion in the words of the problem.

## CI for the mean

$$\bar{X} \pm t_{\alpha/2} \frac{s}{\sqrt{n}}$$

## t-Test for two independent samples

(assume equal variances)

$$H_0 : \mu_1 - \mu_2 = d_0$$

$$t = \frac{\bar{X}_1 - \bar{X}_2 - d_0}{s_p \sqrt{1/n_1 + 1/n_2}}$$

$$s_p = \sqrt{\frac{s_1^2(n_1 - 1) + s_2^2(n_2 - 1)}{n_1 + n_2 - 2}}, \quad \text{df} = n_1 + n_2 - 2$$

## CI for $\mu_1 - \mu_2$

$$\bar{X}_1 - \bar{X}_2 \pm t_{\alpha/2} s_p \sqrt{1/n_1 + 1/n_2}$$

## **z-Test for proportion**

**Step 1.** Null Hypothesis  $H_0 : p = p_0$

**Step 2.** Alternative Hypothesis  $H_1 : p \neq p_0$  two-sided

**Step 3.** Critical value:  $z_{\alpha/2}$

**Step 4.** Test Statistic  $z = \frac{\sqrt{n}(\hat{p} - p_0)}{\sqrt{p_0 q_0}}$

**Step 5.** Decision Rule: Reject  $H_0$  if  $|z| > z_{\alpha/2}$

**Step 6.** (optional) p-value  $2 \times P(Z > |z|)$

Reject  $H_0$  when p-value  $< \alpha$

**Step 7.** Conclusion in the words of the problem.

**Note:** Z-test is valid when  $np_0 q_0 > 5$

**CI for the proportion:**

$$\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}\hat{q}}{n}}$$