

1. Given the position function of an object  $\vec{r}(t) = t^3\mathbf{i} + 6t^2\mathbf{j} + \sin t\mathbf{k}$  with  $0 \leq t \leq \pi$  find the velocity and acceleration vectors.
2. Let  $\vec{u} = \langle 3, -2, -1 \rangle$  and  $\vec{v} = \langle 5, -3, -5 \rangle$ 
  - a. Find a unit vector in the direction of  $\vec{u}$
  - b. Find  $\vec{u} \cdot \vec{v}$ .
  - c. Find  $\vec{u} \times \vec{v}$ .
  - d. Find the projection of  $\vec{v}$  onto  $\vec{u}$ .
  - e. Find the angle between  $\vec{u}$  and  $\vec{v}$ .
  - f. Find a vector parallel to  $\vec{v}$  with length 5 units.
  - g. Compute the lengths of the diagonals of the parallelogram determined by  $\vec{u}$  and  $\vec{v}$ .
  - h. Find a vector orthogonal to both  $\vec{u}$  and  $\vec{v}$ .
  - i. Compute the area of the parallelogram determined by  $\vec{u}$  and  $\vec{v}$ .
2. Find a vector equation of the line that passes through the points  $(2, 6, -1)$  and  $(-6, 4, 0)$ .
3. Find the parametric equations of the line that passes through the point  $(0, 1, 1)$  and parallel to the vector  $\langle 2, -1, 3 \rangle$ .
4. Find a vector equation of the line that passes through  $(2, 1, 0)$  and perpendicular to both  $\mathbf{i} + \mathbf{j}$  and  $\mathbf{j} + \mathbf{k}$ .
5. Find the equation of the plane through  $A(-1, 6, -5)$  and parallel to the plane  $x + y + z + 2 = 0$ .
6. Find an equation of the plane through  $P(-2, 3, 1)$ ,  $Q(1, 1, 0)$ , and  $R(-1, 0, 1)$ .
7. Find the equation of the sphere with center  $(2, -3, 4)$  and tangent to the  $xz$ -plane.
8. Find the equation of the sphere with the line segment  $(1, 5, -2)$  and  $(3, 9, -1)$  is the diameter.
9. Find the distance between the points  $P(1, 2, -3)$  and  $Q(4, 7, -3)$ .
10. Find an equation of the line of intersection of the two plane  $y - 5z = 3$  and  $6x - 7y = 5$ .
11. Find an equation of the line tangent to the curve  $\vec{r}(t) = \langle \sin 2t, \cos 2t, t \rangle$  at  $t = \frac{\pi}{4}$

12. Determine the distance from the point  $P(-6, 3, 0)$  to the line given by  $\vec{r}(t) = \langle 3 + 4t, -2 + 6t, t \rangle$ .
13. Show that the lines with equation  $\vec{r}(t) = \langle 2t - 1, 3 - 4t, 2 + 5t \rangle$   
 $\vec{R}(s) = \langle 4 + 3s, 2s - 1, 3s \rangle$   
 are skew, find the equations of the parallel planes containing the lines, and find the distance between the lines.
14. Let  $\mathbf{r}(t) = \langle \sqrt{2-t}, (e^t - 1)/t, \ln(t+1) \rangle$ .
- Find the domain of  $\mathbf{r}$ .
  - Find  $\lim_{t \rightarrow 0} \vec{r}(t)$
15. Given the points  $A(1, 0, 1)$ ,  $B(2, 3, 0)$  and  $C(-1, 1, 4)$ , find the area of the triangle with vertices  $A$ ,  $B$ , and  $C$ .
16. Find the length of the curve  $\vec{r}(t) = \langle 2t^{3/2}, \cos 2t, \sin 2t \rangle$  for  $0 \leq t \leq 1$ .
17. Find the distance from the point  $(2, 0, -3)$  to the plane  $3x - 4y + 5z = 1$ .
18. A particle moves in space with parametric equations  $x = t, y = t^2, z = \frac{4}{3}t^{3/2}$ . Find the curvature of its trajectory, the unit tangent vector, and the unit normal vector when  $t = 1$ .
19. Find the binormal vector for  $x = t, y = t^2, z = \frac{4}{3}t^{3/2}$  at  $t = 1$ .
20. Find the distance from the point  $(-6, 3, 0)$  to the line given by  $\vec{r}(t) = \langle 1 + 5t, -6 + t, -4t \rangle$
21. A particle starts at the origin with initial velocity  $\mathbf{i} - \mathbf{j} + 3\mathbf{k}$ . Its acceleration is  $\mathbf{a}(t) = 6t\mathbf{i} + 12t^2\mathbf{j} - 6t\mathbf{k}$ . Find its position function.
22. Find the tangential and normal components of acceleration for a particle moving along a conical helix defined by  $\vec{r}(t) = \langle t \cos t, t \sin t, t \rangle$ .
23. The helix  $\mathbf{r}_1(t) = \cos t \mathbf{i} + \sin t \mathbf{j} + t \mathbf{k}$  intersects the curve  $\mathbf{r}_2(t) = (1+t)\mathbf{i} + t^2\mathbf{j} + t^3\mathbf{k}$  at point  $(1, 0, 0)$ . Find the angle of intersection of these curves.

For additional problems, check out the review problems for Chapters 11. Note the questions above are simply a sample of questions possible for the exam; it is possible that other types of questions may appear on your exam.