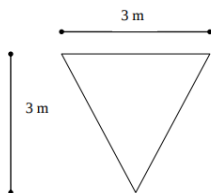


- Find the area of the region bounded by  $y = \frac{1}{2}x$ ,  $y = \sqrt{x-3}$ , and the  $x$ -axis.
- The region  $R$  in the first quadrant bounded by the parabolas  $y = 2 - x^2$  and  $y = x^2$  is revolved about the  $x$ -axis to produce a half-donut shaped solid. Find the volume of the solid in the following ways.
  - Apply the disk method.
  - Apply the shell method.
- Find the volume of the solid of revolution generated by revolving each of the regions below about the specified axis.
  - The region bounded by the graphs of  $y = x^2$  and  $y = x + 2$ , about the line  $x = 3$
  - The same region as part (a), about the line  $y = -1$ .
  - The region bounded by the graphs of  $y = e^x$ ,  $x = 0$  and  $y = \pi$ , about the  $x$  axis.
- Find the arc length of the following curves.
  - $y = (4 - x^{2/3})^{3/2}$  for  $0 \leq x \leq 2$ .
  - $y = \sqrt{1 - x^2}$  for  $-\frac{1}{2} \leq x \leq \frac{1}{2}$
- Find the surface area of the resulting surface of revolution generated by revolving each of the curves below about the specified axis.
  - $f(x) = \sqrt{25 - x^2}$ , for  $0 \leq x \leq 5$ , about the  $y$ -axis.
  - $g(x) = \cos x$ , for  $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$ , about the  $x$ -axis.
- Find the mass of a thin copper rod 1 meter long, made of an alloy with density  $\rho(x) = (8 - 3x)^2$ , where  $x$  is the distance (m) from the left end of the rod.
- A tank is in the shape of a hemisphere, with the top of the tank a circle of radius 5 ft. If the tank is half-full of a liquid with density  $\rho$ , find the work required to pump the water to a level 1 ft above the top of the tank. (Leave your answer in terms of  $\rho$  and  $g$ .)
- A water trough is 10 m long, with a triangular shaped cross-section. The length of this triangular cross-section is 3 m, and its height is also 3 m. How much work is required to pump the water out of the top of the tank? (Use  $\rho g = 9800$ .)



9. Find the hydrostatic force exerted on the face of a dam filled with water, whose shape is given by each description below.

a. The face is shaped like a trapezoid. The length of the base is 12m, the length of the top is 18m with a height of 6m.

b. The face is shaped like the lower-half of a circle of radius 4m.

10. Evaluate the following integrals.

a.  $\int \frac{e^{2x}}{4 + e^{2x}} dx$

b.  $\int \tan(5x) dx$

c.  $\int \frac{e^{\sqrt{x}}}{\sqrt{x}} dx$

d.  $\int 7^{2x} dx$

e.  $\int \frac{\cosh(\ln x)}{x} dx$

f.  $\int_0^1 \cosh^3(x) \sinh(x) dx$

11. Compute  $\frac{d}{dx}$  of the following functions.

a.  $f(x) = x^{\tan x}$

b.  $f(x) = \left(\frac{1}{x}\right)^x$