

**Guidelines**

- **Calculators are not allowed.**
  - Read the questions carefully. You have 65 minutes; use your time wisely.
  - You may leave your answers in symbolic form, like  $\sqrt{3}$  or  $\ln(2)$ , unless they simplify further like  $\sqrt{9} = 3$  or  $\cos(3\pi/4) = -\sqrt{2}/2$ .
  - Put a box around your final answers when relevant.
  - Show all steps in your solutions and make your reasoning clear. Answers with no explanation will not receive full credit, even when correct.
  - Use the space provided. If necessary, write “see other side” and continue working on the back of the same page.
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1. (8 points) To be completed once exams are graded and returned. Please correct any problem with points deducted. All corrections should be completed neatly on a separate sheet of paper. Once you have finished your corrections, take your exam and corrections to the Office of Student Learning (OSL), and a tutor will check your answers and sign below. The checked solutions should be given to your instructor.

Signature: \_\_\_\_\_

Print Name: \_\_\_\_\_

Date: \_\_\_\_\_

2. For the point with rectangular coordinates  $(-1, \sqrt{3})$ , find polar coordinates with
- (3 points)  $r > 0$  and  $0 \leq \theta < 2\pi$ ;
  - (3 points)  $r < 0$  and  $0 \leq \theta < 2\pi$ .
3. (8 points) Convert the polar equation  $r = 2 \cos \theta - 6 \sin \theta$  to rectangular coordinates and describe the curve it represents.
4. (8 points) Sketch the polar curve  $r = \frac{1}{2} - \sin \theta$ .

5. (8 points) Set up, but do not evaluate, an integral representing the area enclosed by the inner loop of  $r = \frac{1}{2} - \sin \theta$ .

6. Consider the parametric equations  $x = e^t$ ,  $y = 3e^{-2t}$  for  $0 \leq t \leq \ln 3$ .

a. (6 points) Eliminate the parameter to obtain an equation in  $x$  and  $y$ .

b. (4 points) Sketch the curve.

7. Write each complex number in the form  $x + yi$ .

a. (4 points)  $i^{77}$

b. (4 points)  $\frac{2 - 3i}{-1 + 5i}$

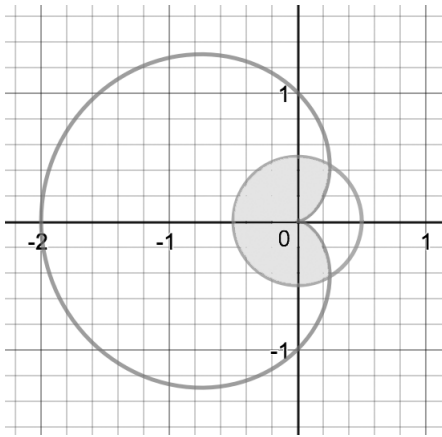
8. (8 points) Find the point  $(x, y)$  where the tangent line to the parametric curve  $x = t^2 - 9$ ,  $y = t^2 - 8t$  is horizontal.

9. (8 points) Find an equation of the tangent line to the polar curve  $r = 8 \sin \theta$  at  $\theta = \frac{5\pi}{6}$ .

10. (8 points) Write  $(-1 + i)^8$  in the form  $x + yi$  without expanding.

11. (8 points) Find all complex cube roots of  $-27$ .

12. (12 points) Calculate the area inside both the cardioid  $r = 1 - \cos \theta$  and the circle  $r = \frac{1}{2}$ .



Question	Points	Score
1	8	
2	6	
3	8	
4	8	
5	8	
6	10	
7	8	
8	8	
9	8	
10	8	
11	8	
12	12	
Total:	100	