- 1. Write an equation of the line that passes through (-3,7) and is perpendicular to the line with equation y-2x=10.
- 2. Simplify each of the following:

a. 
$$\frac{\frac{1}{2+h} - \frac{1}{2}}{h}$$
  
b. 
$$\frac{x^{-2/5}\sqrt{4x}}{\sqrt[3]{x}}$$

3. Solve the inequality  $\frac{x^2 - 9}{x - 1} \le 0$ ; express the domain in interval notation.

4. For the function 
$$f(x) = 3x - 6$$
, find  $\frac{f(x+h) - f(x)}{h}$ 

5. Determine each of the following (if they exist) :

a. sin(0)

- b.  $\cos(0)$
- c.  $\sin^{-1}(4)$
- d.  $\tan^{-1}(1)$
- 6. Write sin(arctan x) as an algebraic function that does not involve a trigonometric function or inverse trigonometric function.
- 7. Sketch a graph of each of the following. Label any important points or features.
  - a.  $\sin x$

b. 
$$\sqrt{x-3}$$

- 8. Give the formal definition of the limit statement  $\lim_{x\to c} f(x) = L$ . Illustrate the definition with a graph.
- 9. Evaluate each of the following, if they exist:

a. 
$$\lim_{x \to 1} \left( \frac{1+3x}{1+4x^2+3x^4} \right)^3$$
, state which limit laws were used.  
b. 
$$\lim_{x \to \infty} e^{-x} \tan^{-1} x$$
c. 
$$\lim_{x \to 2} \frac{x^2+2x-8}{x^4-16}$$
d. 
$$\lim_{x \to 3} \frac{\frac{1}{x-3} - \frac{1}{x}}{x-3}$$
e. 
$$\lim_{x \to 8^-} \frac{|x-8|}{x-8}$$
f. 
$$\lim_{x \to \infty} \frac{\sqrt{x}}{1-\sqrt{x}}$$

g. 
$$\lim_{x \to 0} \frac{3x}{\sin 2x}$$
  
h. 
$$\lim_{x \to 3} f(x) \text{ where } f(x) = \begin{cases} 2(x+1) & \text{if } x < 3\\ 4 & \text{if } x = 3\\ x^2 - 1 & \text{if } x > 3 \end{cases}$$

- 10. Use the Intermediate Value Theorem to show that  $x^4 + x 3 = 0$  on [1, 2].
- 11. Use the definition of continuity to find constant c to such that  $f(x) = \begin{cases} x^2 c^2 & \text{if } x < 4 \\ cx + 20 & \text{if } x \ge 4 \end{cases}$  is continuous at x = 4.
- 12. Describe the interval(s) on which the function  $f(x) = \begin{cases} \frac{x^2 1}{x 1} & \text{if } x < 1\\ 0 & \text{if } x = 1 \text{ is continuous.} \text{ At any point } \\ 3x 1 & \text{if } x > 1 \end{cases}$

where f fails to be continuous use limits to determine the type of discontinuity.

- 13. Find the roots, discontinuities and horizontal and vertical asymptotes of the following functions. Support your answers by explicitly computing any relevant limits.
  - a.  $f(x) = \frac{(x+1)(x-2)}{(x-2)^2(x+2)}$ b.  $f(x) = \frac{4^x - 6(2^x) + 5}{1 - 2^x}$
- 14. Sketch the graph of an example of a function *f* that satisfies the following conditions.

$$\lim_{x \to 0^+} f(x) = -2 \qquad \lim_{x \to 0^-} f(x) = 1 \qquad f(0) = -1$$
$$\lim_{x \to 2^+} f(x) = -\infty \qquad \lim_{x \to 2^-} f(x) = +\infty$$
$$\lim_{x \to \infty} f(x) = 3 \qquad \lim_{x \to \infty} f(x) = 4$$

15. Using the graph of f(x), answer each of the following:



a. 
$$\lim_{x \to 7} f(x)$$
  
b.  $\lim_{x \to 1^{-}} f(x)$ 

c. Where is f(x) not continuous?

Topics:

- ✓ Review algebra and trig from chapter 0:
  - o Lines
  - Inverse functions
  - Trig functions /Inverse Trig functions
  - Exponential and Logarithmic Functions
- ✓ Limits:
  - Graphical, numerical and algebraic techniques for finding limits; be sure you know how to use limit laws (think about the five problems we did in class asking you to state the laws used).
  - Infinite limits; when *y* becomes arbitrarily large in magnitude as *x* approaches *a*.
  - $\circ$  End behavior; what happens to y as x becomes arbitrarily large in magnitude.
  - Continuity

For additional problems, check out the review problems for Chapters 0 and 1. Note the questions above are simply a sample of questions possible for the exam; it is possible that other types of questions may appear on your exam.