- 1. Find an equation of a line who passes through the points (-4, 2) and (2, 7).
- 2. Solve the equation for x: x(x-1)=12
- 3. Solve the equation for  $x: x^2 + 6x + 8 < 0$

4. Express the domain of the following function in interval notation:  $f(x) = \sqrt{\frac{x-2}{x+2}}$ 

- 5. If  $f(x) = x x^2$ , find  $\frac{f(2+h) f(2)}{h}$  and simplify.
- 6. Find  $\cos(\arcsin x)$
- 7. Suppose  $\cos \theta = -\frac{3}{5}$  for  $\frac{\pi}{2} < \theta < \pi$ , find a.  $\tan \theta$ 
  - b.  $\sin(2\theta)$

8. Give the vertical and horizontal asymptotes of  $f(x) = \frac{x^2 - 9}{x^2 - x - 6}$ .

9. Using the Basic Properties of Limits, evaluate the following limits:

a. 
$$\lim_{x \to 3} \frac{x^2 + 4x - 21}{x - 3}$$
  
b. 
$$\lim_{x \to 1^+} \sqrt{\frac{x^2 + 2x - 3}{x - 1}}$$
  
c. 
$$\lim_{x \to -3} \frac{2 - \sqrt{x^2 - 5}}{x + 3}$$
  
d. 
$$\lim_{x \to 5^-} \frac{|x - 5|}{x - 5}$$
  
e. 
$$\lim_{x \to \infty} \frac{3x^2 - 2x + 1}{(x - 2)^2}$$
  
f. 
$$\lim_{x \to 2} f(x)$$
, where  $f(x) = \begin{cases} 3 - 2x & \text{if } x < 2\\ 2 & \text{if } x = 2\\ x^2 - 5 & \text{if } x > 2 \end{cases}$ 

10. Explain why  $f(x) = x^3 + 2x + 5$  has a zero in the interval  $-2 \le x \le 0$ .

11. Let  $f(x) = \begin{cases} ax+3 & \text{if } x > 5 \\ 8 & \text{if } x = 5 \text{, find } a \text{ and } b \text{ such that } f \text{ is continuous at } x = 5. \text{Use the definition of } \\ x^2 + bx + 1 & \text{if } x < 5 \end{cases}$ 

continuity in your answer.

12. Sketch a function that satisfies the following conditions: f(0) = 1  $\lim_{x \to \pm \infty} f(x) = 0$ ,  $\lim_{x \to 2^-} f(x) = \infty$   $\lim_{x \to 2^+} f(x) = \infty$ 

- 13. Explain why or why not. Determine whether the following statements are true and give an explanation or counterexample.
  - a. The rational function  $\frac{x-1}{x^2-1}$  has vertical asymptotes at x = -1 and x = 1.
  - b. The value of  $\lim_{x \to a} f(x)$ , if it exists is found by calculating f(a).
  - c. If  $\lim_{x \to a} f(x)$  does not exist, then either  $\lim_{x \to a} f(x) = +\infty$  or  $\lim_{x \to a} f(x) = -\infty$ .
  - d. If  $\lim_{x \to a} f(x) = +\infty$  or  $\lim_{x \to a} f(x) = -\infty$ ,  $\lim_{x \to a} f(x)$  does not exist.
  - e. For linear functions, the slope of any secant line always equals the slope of any tangent line.

## **Limit Laws**

Suppose that k is a constant and the limits  $\lim_{x\to c} f(x)$  and  $\lim_{x\to c} g(x)$  exist. Then

- 1. Constant Multiple:  $\lim_{x \to c} kf(x) = k \lim_{x \to c} f(x)$
- 2. Sum/Difference Rule:  $\lim_{x \to c} [f(x) \pm g(x)] = \lim_{x \to c} f(x) \pm \lim_{x \to c} g(x)$
- 3. Product rule:  $\lim_{x \to c} [f(x) \cdot g(x)] = \lim_{x \to c} f(x) \cdot \lim_{x \to c} g(x)$
- 4. Quotient rule:  $\lim_{x \to c} \left[ \frac{f(x)}{g(x)} \right] = \frac{\lim_{x \to c} f(x)}{\lim_{x \to c} g(x)} \text{ if } \lim_{x \to a} g(x) \neq 0$
- 5. Composition Rule:  $\lim_{x \to c} f(g(x)) = f(\lim_{x \to c} g(x))$ , if f is continuous at  $\lim_{x \to c} g(x)$
- 6. Cancellation Theorem for Limits -- If  $\lim_{x \to c} g(x)$  exists and f is a function that is equal to g for all x sufficiently close to c except possibly at c itself, then  $\lim_{x \to c} f(x) = \lim_{x \to c} g(x)$
- 7. The Squeeze Theorem for Limits If  $l(x) \le f(x) \le u(x)$  for all x sufficiently close to c, but not necessarily at x = c, and if  $\lim_{x \to c} l(x) = L = \lim_{x \to c} u(x)$ , then  $\lim_{x \to c} f(x) = L$
- 8. Limits Whose Denominators Approach Zero from the Right or the Left

a. If 
$$\lim_{x \to c} \frac{f(x)}{g(x)}$$
 is of the form  $\frac{1}{0^+}$ , then  $\lim_{x \to c} \frac{f(x)}{g(x)} = \infty$   
b. If  $\lim_{x \to c} \frac{f(x)}{g(x)}$  is of the form  $\frac{1}{0^-}$ , then  $\lim_{x \to c} \frac{f(x)}{g(x)} = -\infty$ 

9. Limits Whose Denominators Become Infinite Approach Zero

a. If 
$$\lim_{x \to \infty} \frac{f(x)}{g(x)}$$
 is of the form  $\frac{1}{\infty}$ , then  $\lim_{x \to \infty} \frac{f(x)}{g(x)} = 0$   
b. If  $\lim_{x \to \infty} \frac{f(x)}{g(x)}$  is of the form  $\frac{1}{-\infty}$ , then  $\lim_{x \to \infty} \frac{f(x)}{g(x)} = 0$   
10.  $\lim_{\theta \to 0} \frac{\sin \theta}{\theta}$ 

Similar results hold for limits at infinity and one-sided limits